Computer Graphics

Bing-Yu Chen National Taiwan University The University of Tokyo

Hidden-Surface Removal

- Back-Face Culling
- □ The Depth-Sort Algorithm
- Binary Space-Partitioning Trees
- The z-Buffer Algorithm
- Visible-Surface Ray Tracing (Ray Casting)
- □ Space Subdivision Approaches

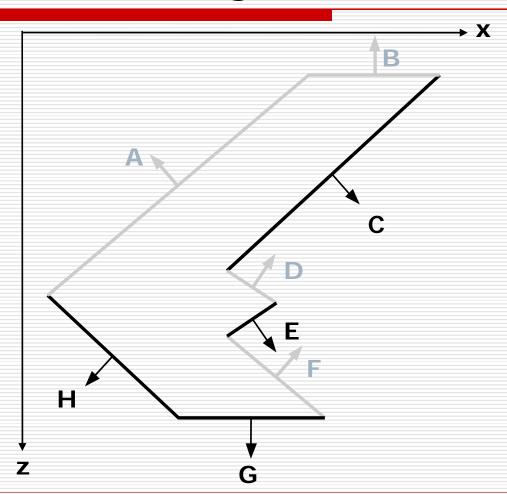
Hidden-Surface Removal = Visible-Surface Determination

- Determining what to render at each pixel.
- □ A point is visible if there exists a direct line-of-sight to it, unobstructed by another other objects (visible surface determination).
- Moreover, some objects may be invisible because there are behind the camera, outside of the field-ofview, too far away (clipping) or back faced (backface culling).

Hidden Surfaces: why care?

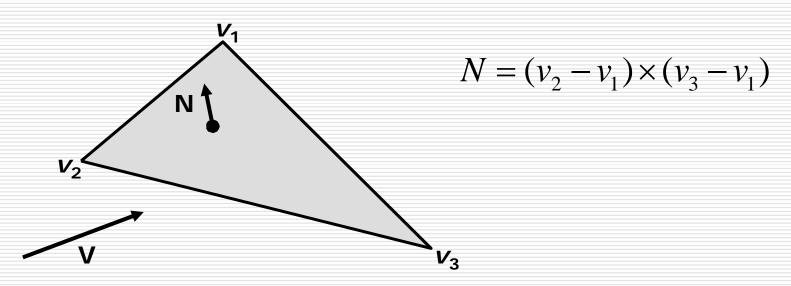
- □ Occlusion: Closer (opaque) objects along same viewing ray obscure more distant ones.
- Reasons for removal
 - Efficiency: As with clipping, avoid wasting work on invisible objects.
 - Correctness: The image will look wrong if we don't model occlusion properly.

Back-Face Culling = Front Facing

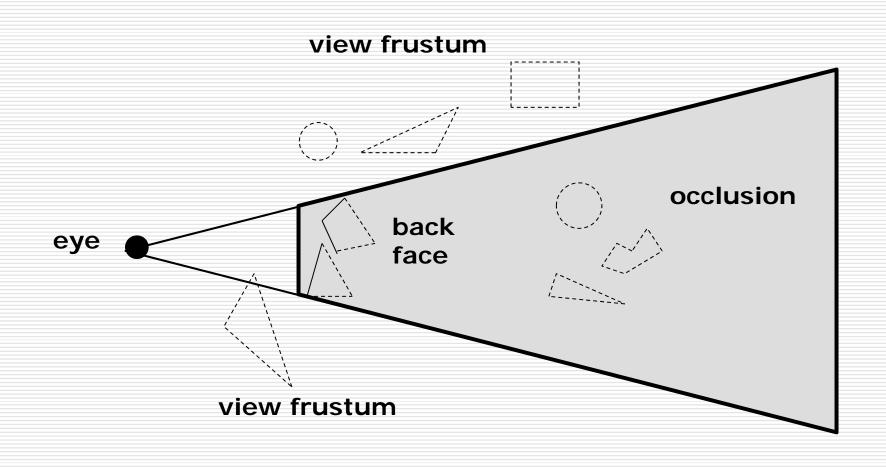


Back-Face Culling = Front Facing

- use cross-product to get the normal of the face (not the actual normal)
- use inner-product to check the facing



Clipping (View Frustum Culling)

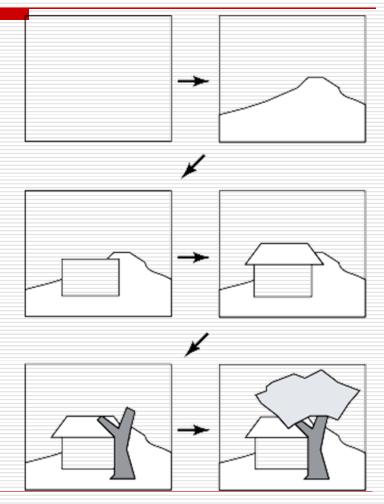


List-Priority Algorithms

- □ The Painter's Algorithm
- The Depth-Sort Algorithm
- Binary Space-Partitioning Trees

The Painter's Algorithm

Draw primitives from back to front need for depth comparisons.



The Painter's Algorithm

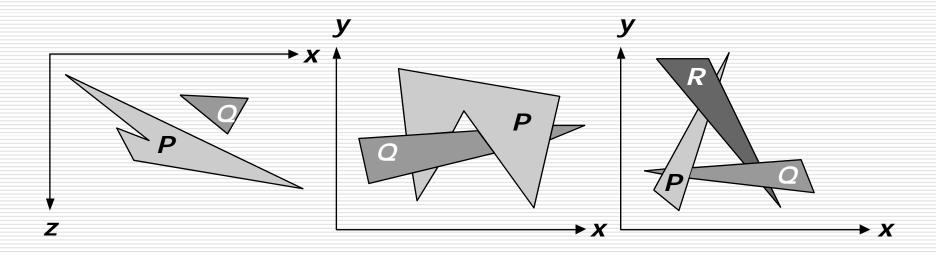
- \Box for the planes with constant z
- □ not for real 3D, just for 2½D

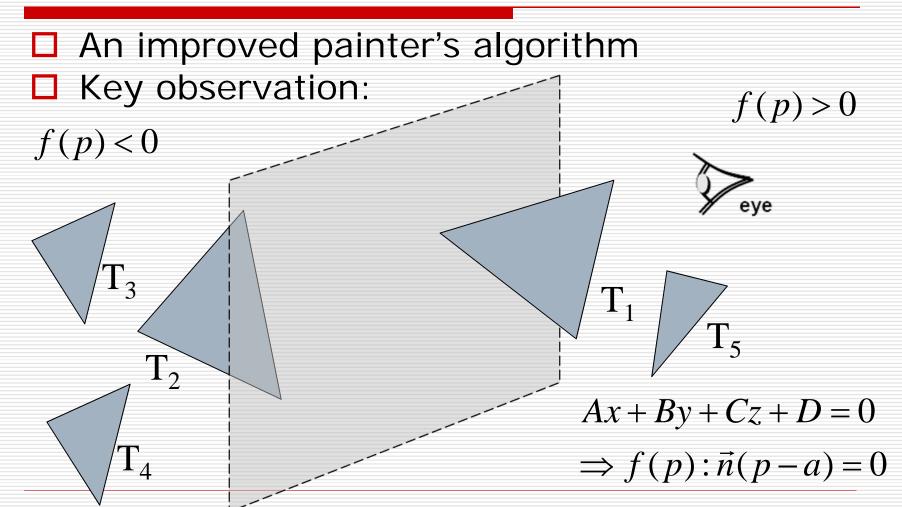
- sort all polygons according to the smallest (farthest) z coordinate of each
- scan convert each polygon in ascending order of smallest z coordinate (i.e., back to front)

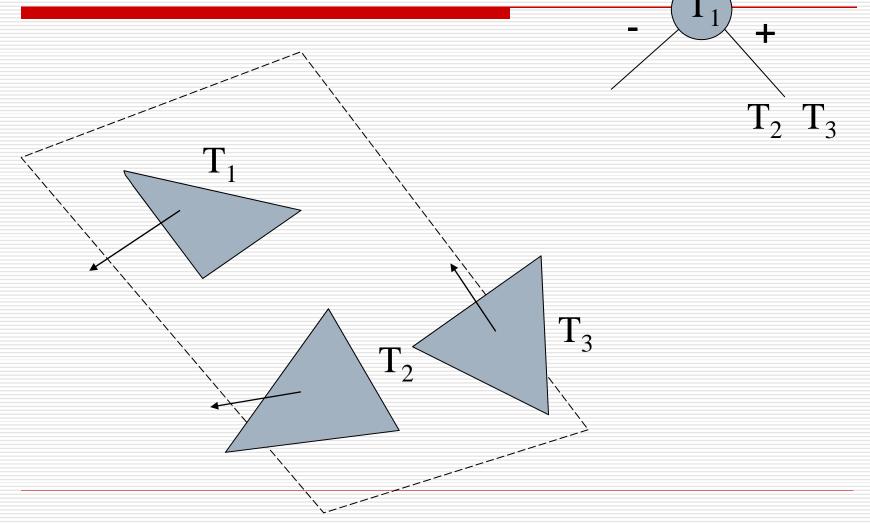
The Depth-Sort Algorithm

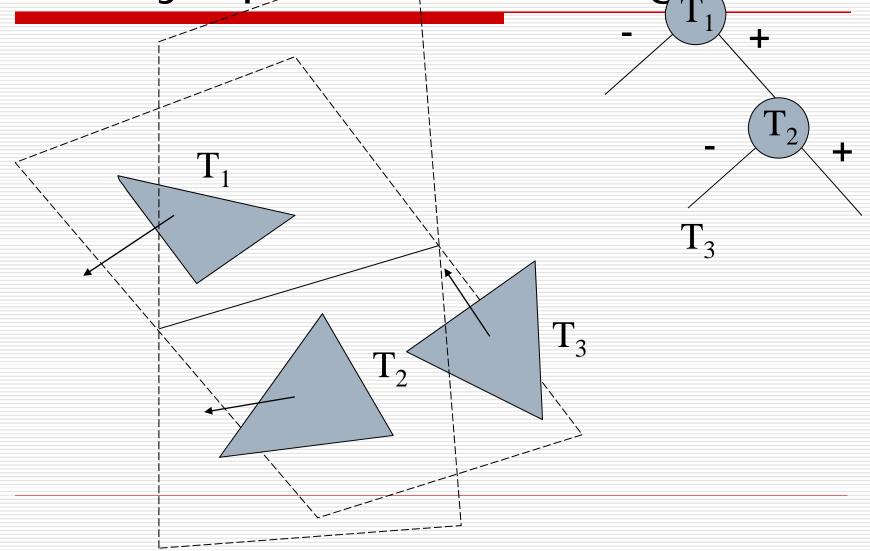
- sort all polygons according to the smallest (farthest) z coordinate of each
- resolve any ambiguities that sorting may cause when the polygons' z extents overlap, splitting polygons if necessary
- scan convert each polygon in ascending order of smallest z coordinate (i.e., back to front)

Overlap Cases

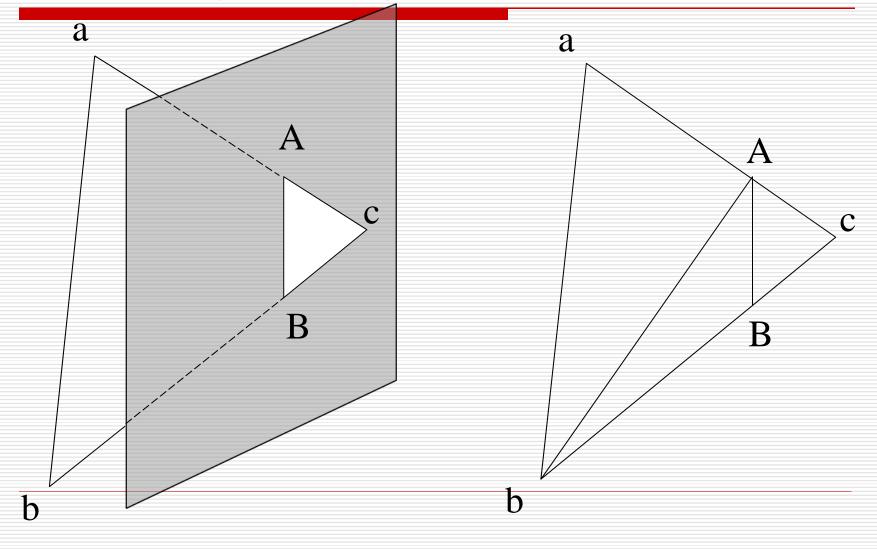








Splitting triangles



BSP Tree Construction

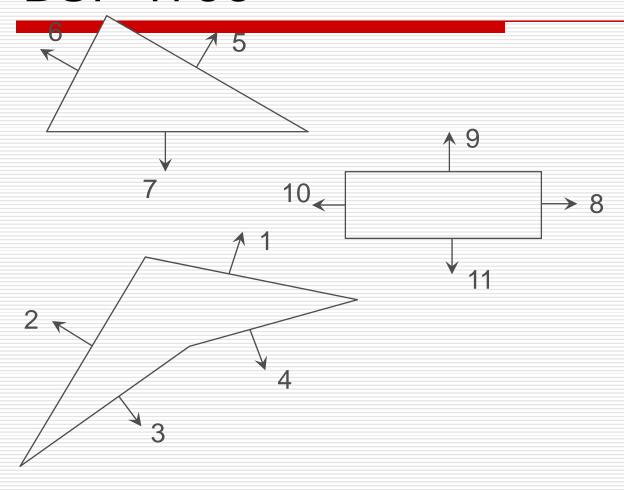
```
BSPtree makeBSP(L: list of polygons) {
   if (L is empty) {
      return the empty tree;
   }
   Choose a polygon P from L to serve as root;
   Split all polygons in L according to P
   return new TreeNode (
      P,
      makeBSP(polygons on negative side of P),
      makeBSP(polygons on positive side of P))
}
```

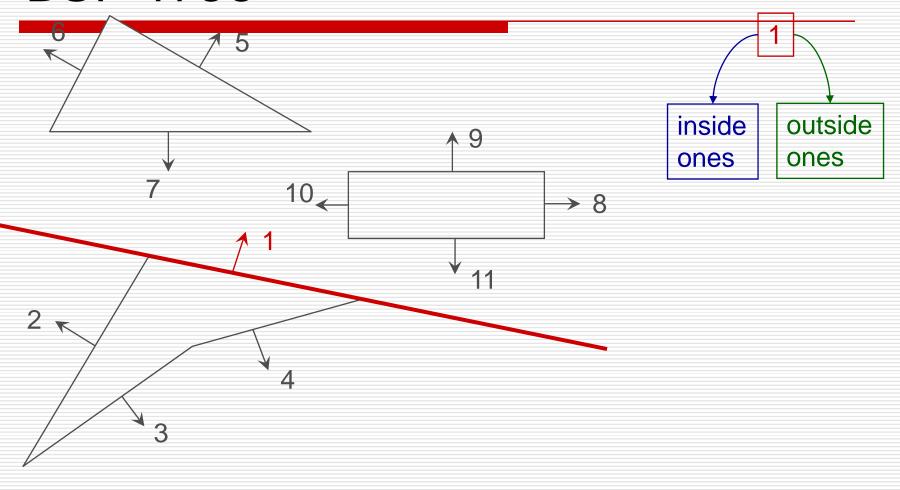
- Splitting polygons is expensive! It helps to choose P wisely at each step.
 - Example: choose five candidates, keep the one that splits the fewest polygons.

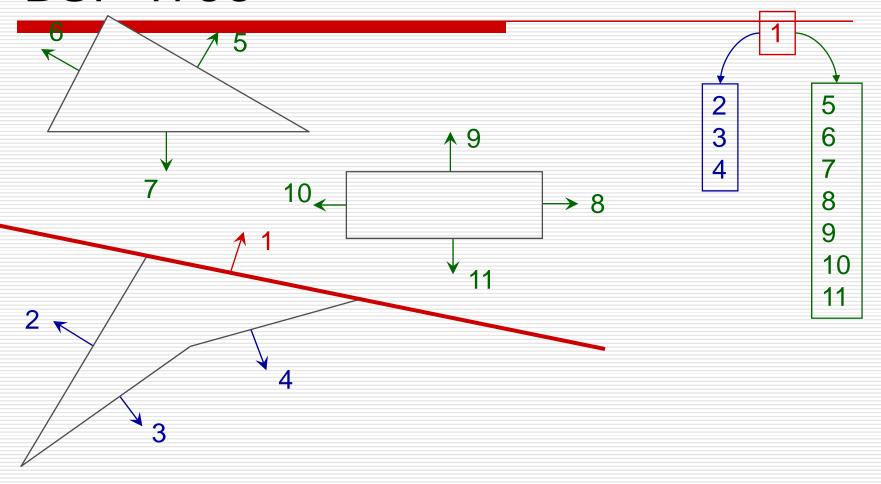
BSP Tree Display

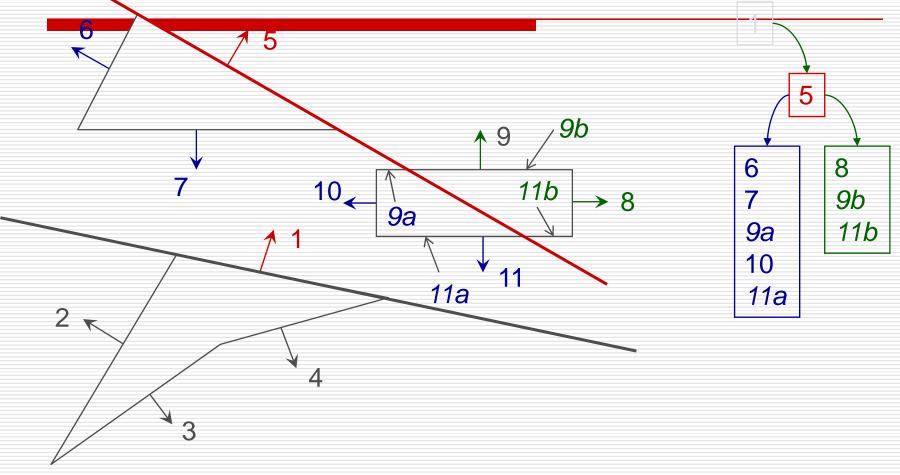
```
void showBSP(v: Viewer, T: BSPtree) {
   if (T is empty) return;
   P = root of T;
   if (viewer is in front of P) {
       showBSP(back subtree of T);
       draw P;
       showBSP(front subtree of T);
   } else {
       showBSP(front subtree of T);
       draw P:
       showBSP(back subtree of T);
```

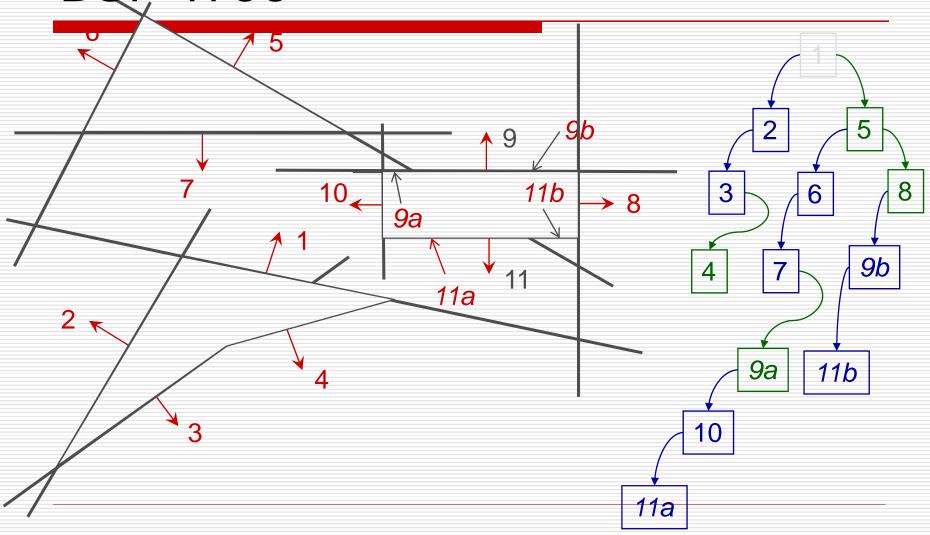
- Same BSP tree can be used for any eye position, constructed only once if the scene if static.
- It does not matter whether the tree is balanced. However, splitting triangles is expensive and try to avoid it by picking up different partition planes.





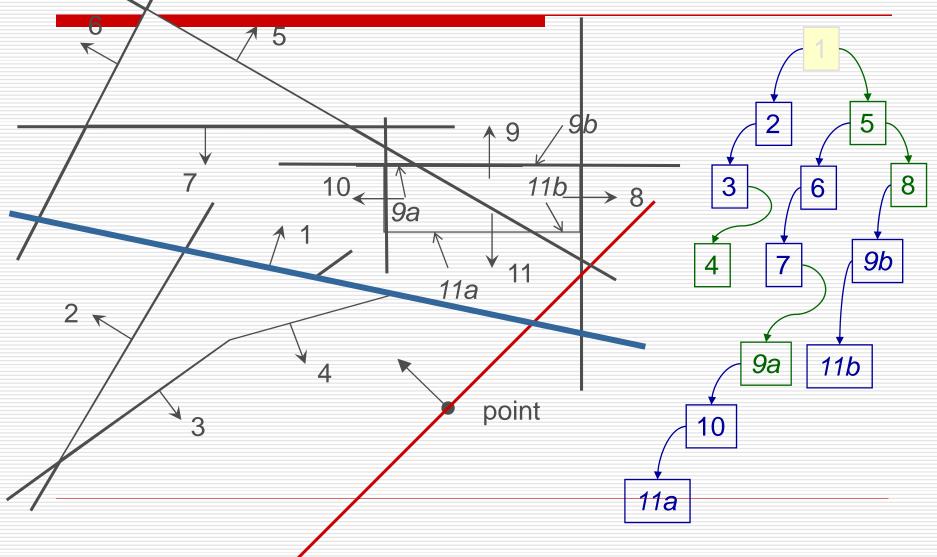




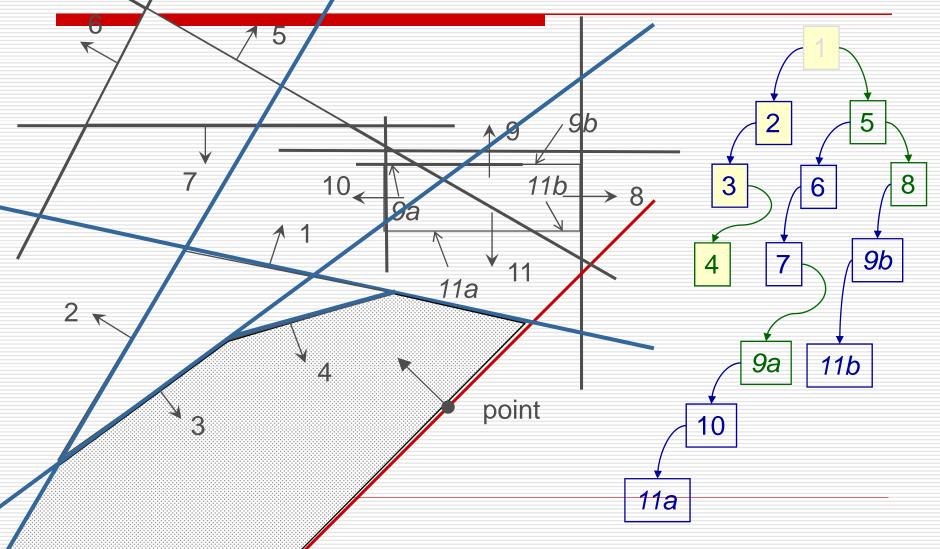


BSP Tree 5 5 **4** 9 10← 11b_ 3 8 6 **→** 8 9*a* 9b 11a 9a 11b point 10 11a

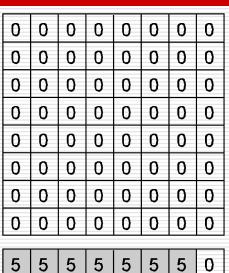
BSP Tree Traversal



BSP, Tree Traversal



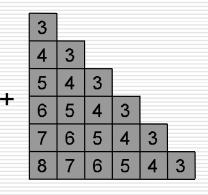
- Resolve depths at the pixel level
- Idea: add Z to frame buffer, when a pixel is drawn, check whether it is closer than what's already in the frame buffer



	5	5	5	5	5	5	5	
	5	5	5	5	5	5		
	5	5	5	5	5			
+	5	5	5	5				
	5	5	5					
	5	5						
	5							

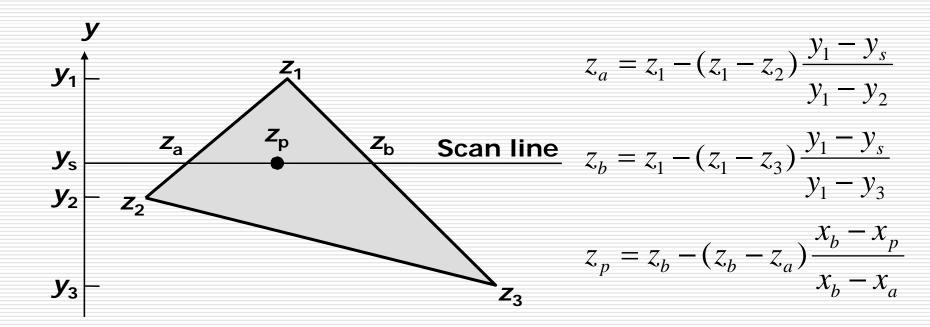
5	5	5	5	5	5	5	0
5	5	5	5	5	5	0	0
5	5	5	5	5	0	0	0
5	5	5	5	0	0	0	0
5	5	5	0	0	0	0	0
5	5	0	0	0	0	0	0
5	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0

5	5	5	5	5	5	5	0
5	5	5	5	5	5	0	0
5	5	5	5	5	0	0	0
5	5	5	5	0	0	0	0
5	5	5	0	0	0	0	0
5	5	0	0	0	0	0	0
5	0	0	0	0	0	0	0
0	0	0	0	0	0	0	0
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5	5	5	5	5	5	5	0
5	5	5	5	5	5	0	0
5	5	5	5	5	0	0	0
5	5	5	5	0	0	0	0
6	5	5	3	0	0	0	0
7	6	5	4	3	0	0	0
8	7	6	5	4	3	0	0
0	0	0	0	0	0	0	0

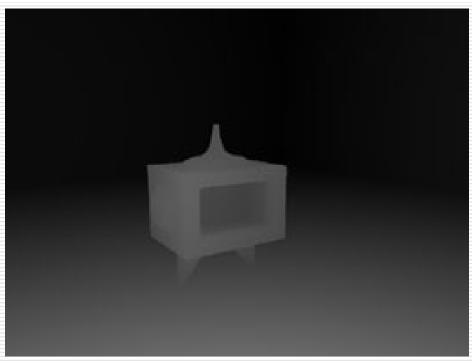
```
void zBuffer() {
   int pz;
   for (each polygon) {
       for (each pixel in polygon's projection) {
              pz=polygon's z-value at (x,y);
              if (pz > = ReadZ(x,y)) {
                     WriteZ(x,y,pz);
                     WritePixel(x,y,color);
```



z-Buffer: Example



color buffer



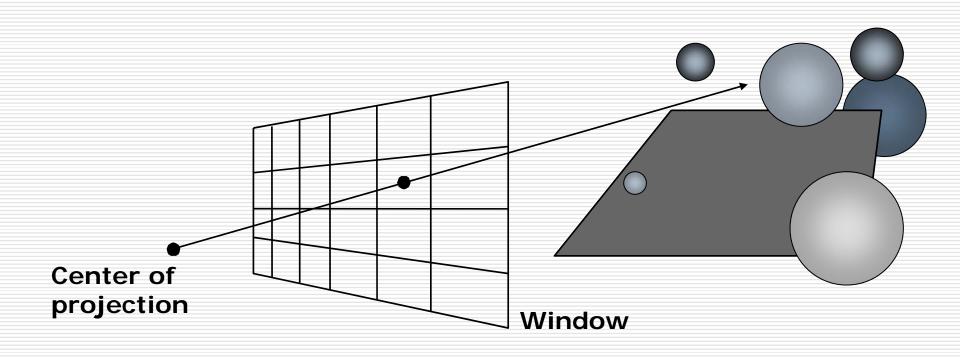
depth buffer

- Benefits
 - Easy to implement
 - Works for any geometric primitive
 - Parallel operation in hardware
 - independent of order of polygon drawn
- Limitations
 - Memory required for depth buffer
 - Quantization and aliasing artifacts
 - Overfill
 - Transparency does not work well

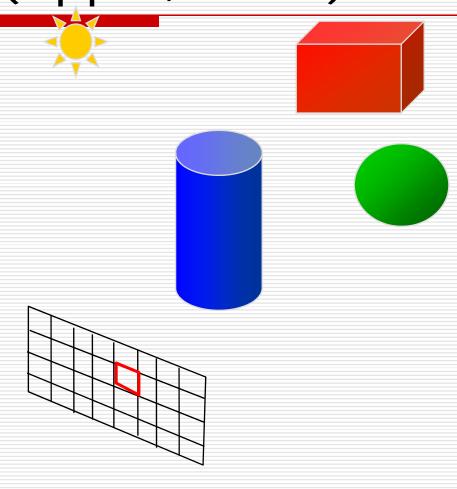
Ray Tracing = Ray Casting

```
select center of projection and window on viewplane;
for (each scan line in image) {
    for (each pixel in scan line) {
        determine ray from center of projection through pixel;
        for (each object in scene) {
                 if (object is intersected and is closest considered thus far)
                          record intersection and object name;
        set pixel's color to that at closest object intersection;
```

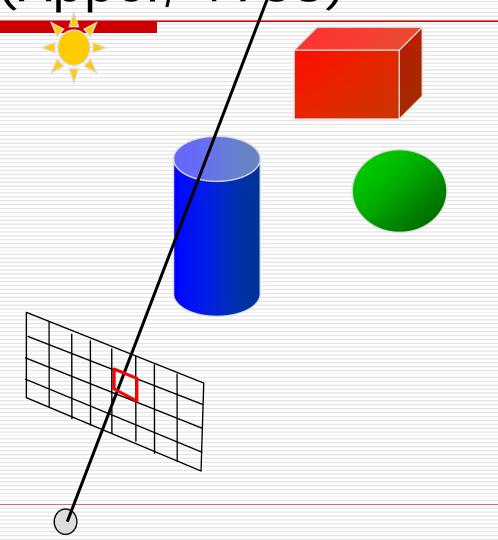
Ray Casting

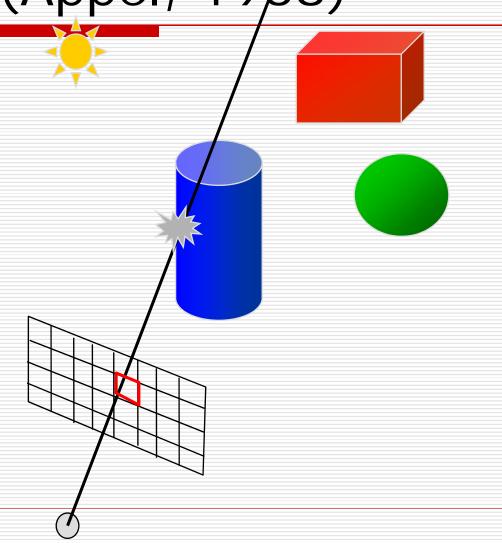


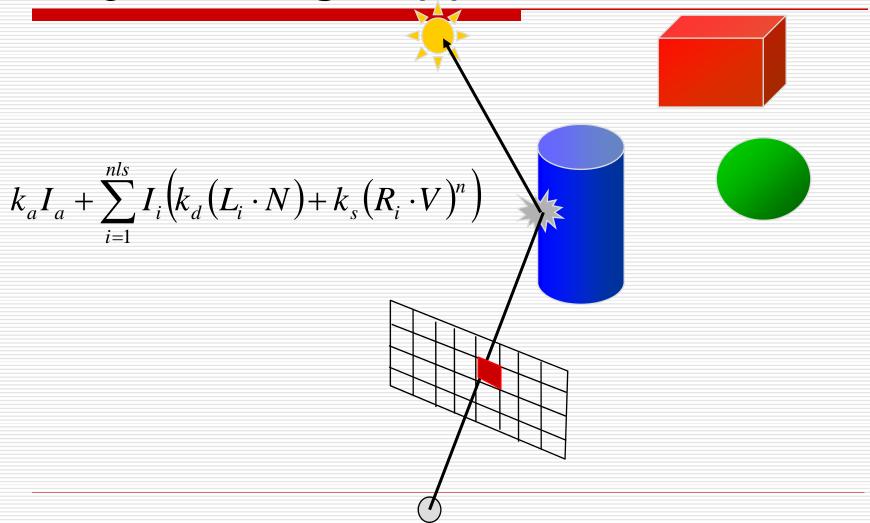
Ray Casting (Appel, 1968)

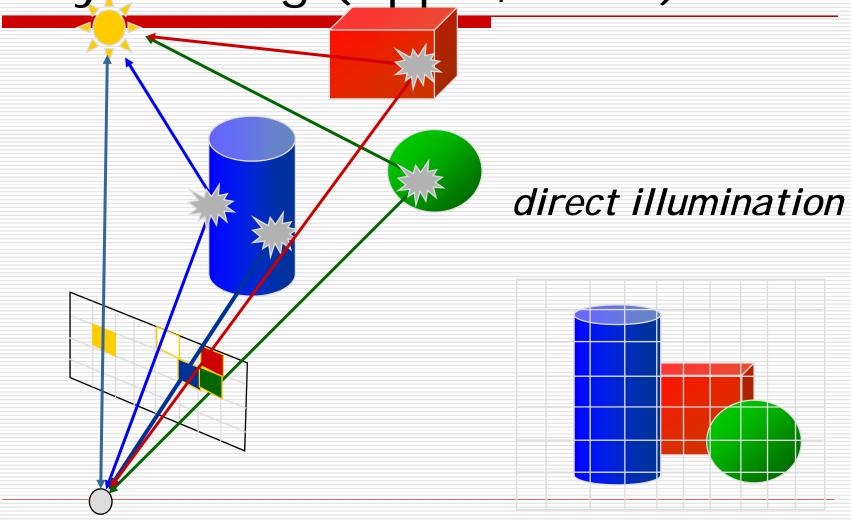




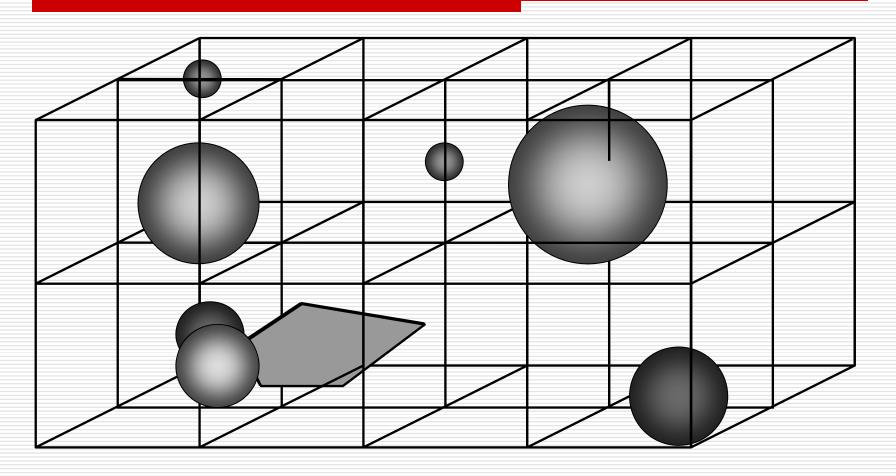




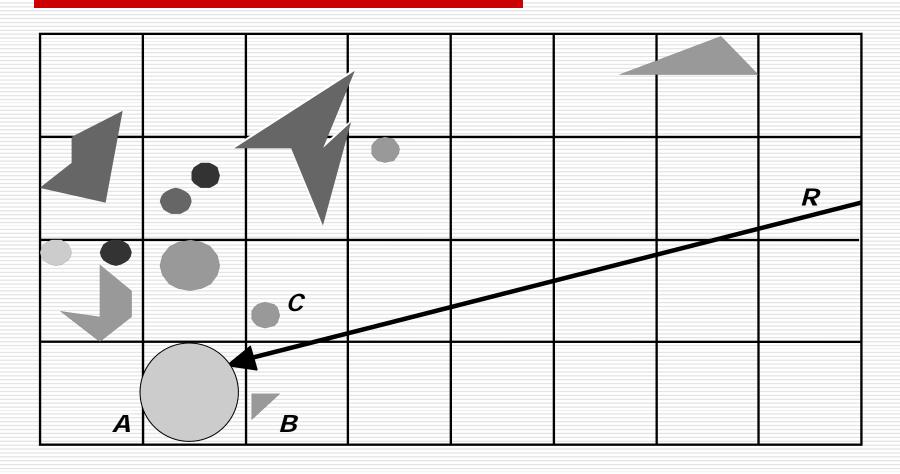




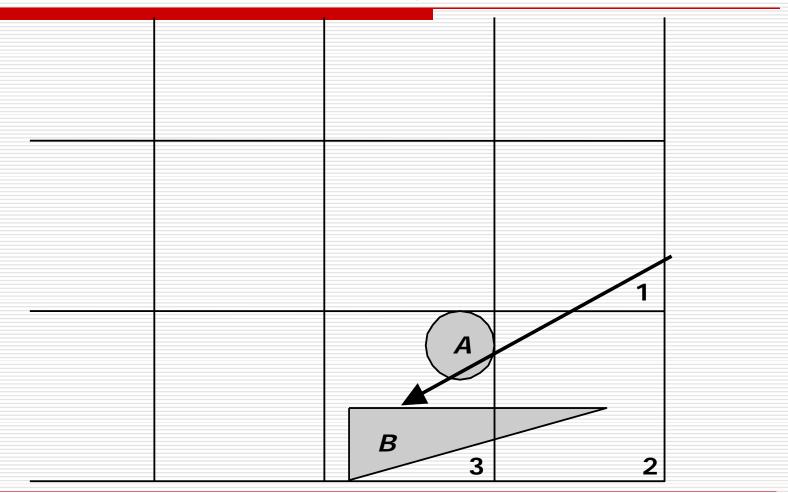
Spatial Partitioning



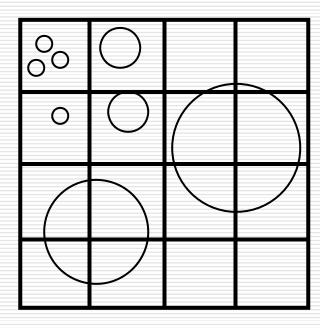
Spatial Partitioning



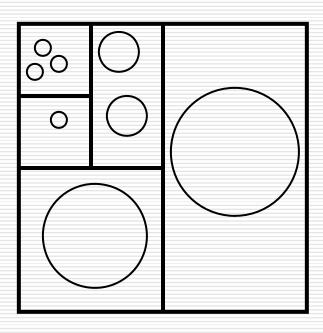
Spatial Partitioning



Space Subdivision Approaches

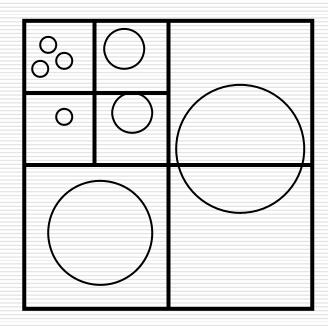


Uniform grid

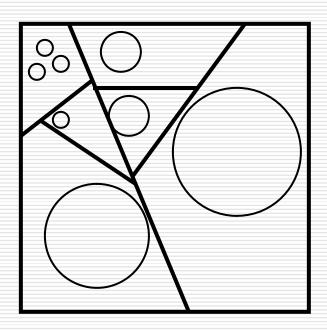


K-d tree

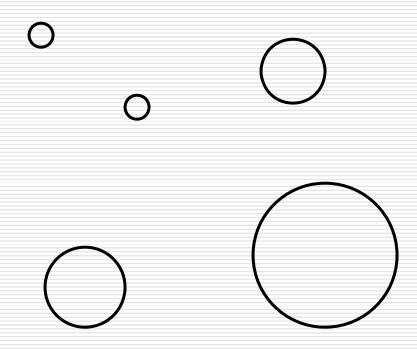
Space Subdivision Approaches

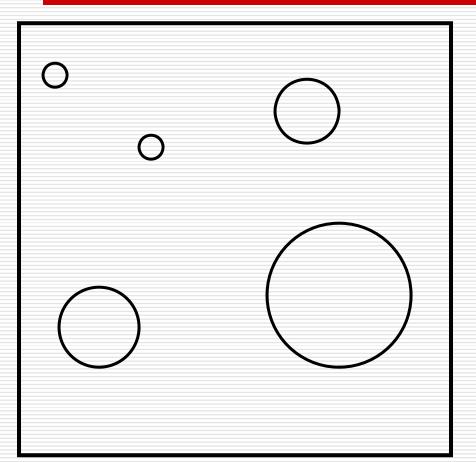


Quadtree (2D) Octree (3D)



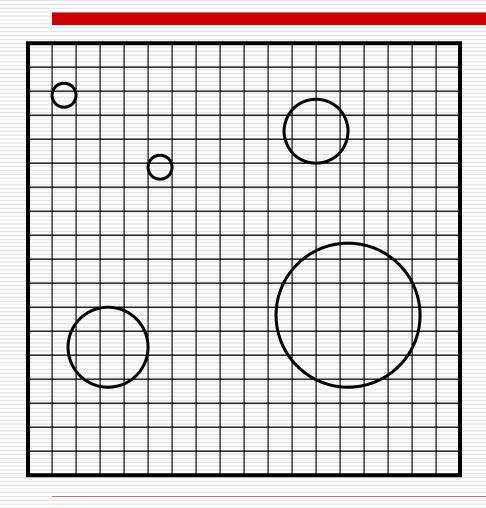
BSP tree





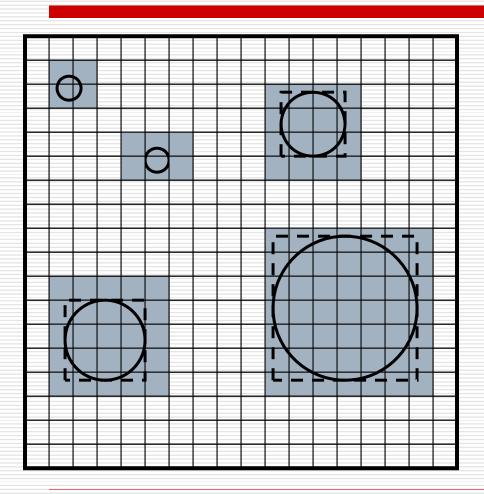
Preprocess scene

1. Find bounding box



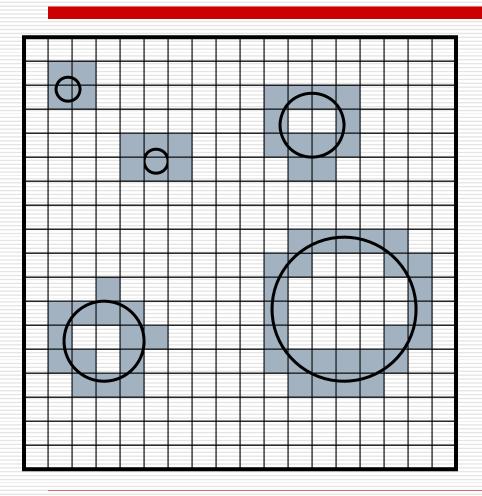
Preprocess scene

- 1. Find bounding box
- 2. Determine grid resolution



Preprocess scene

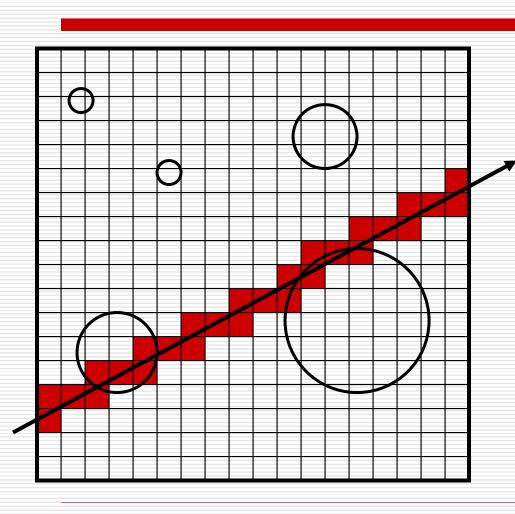
- 1. Find bounding box
- 2. Determine grid resolution
- 3. Place object in cell if its bounding box overlaps the cell



Preprocess scene

- 1. Find bounding box
- 2. Determine grid resolution
- 3. Place object in cell if its bounding box overlaps the cell
- 4. Check that object overlaps cell (expensive!)

Uniform Grid Traversal

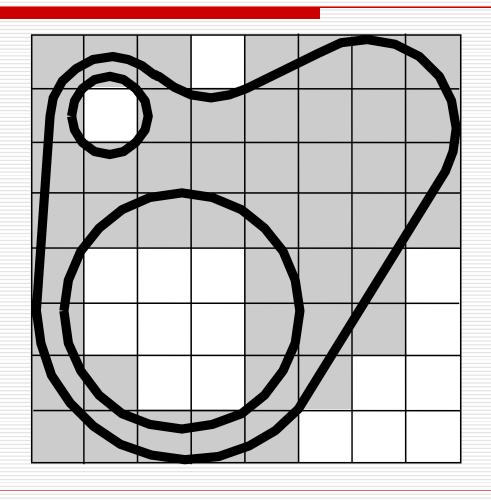


Preprocess scene

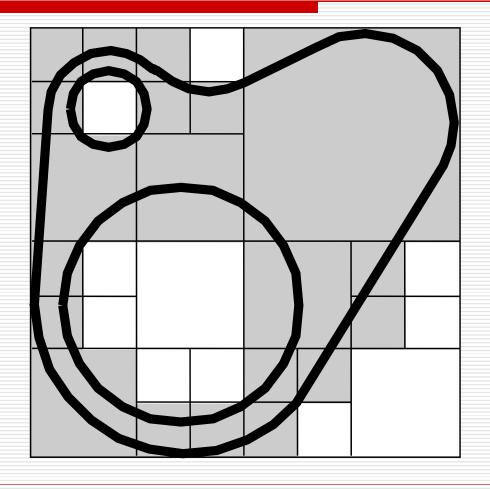
Traverse grid

3D line = 3D-DDA

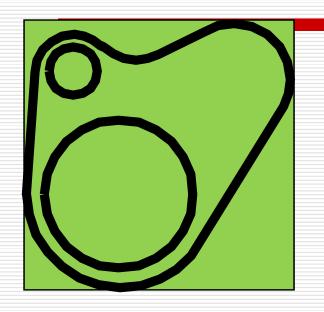
From Uniform Grid to Quadtree



Quadtree (Octrees)



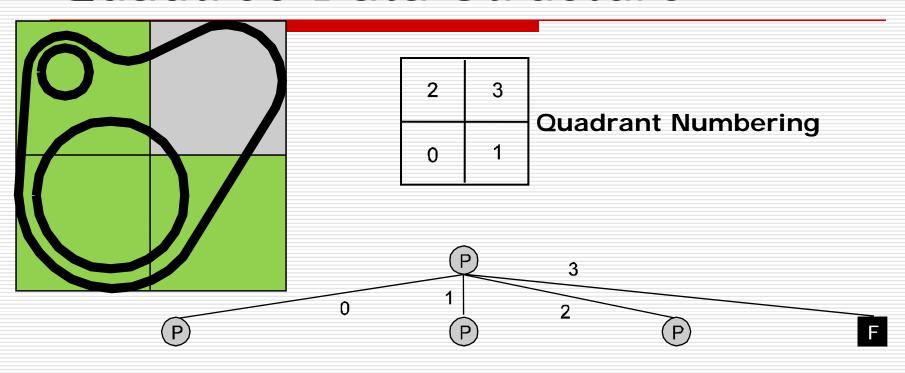
subdivide the space adaptively

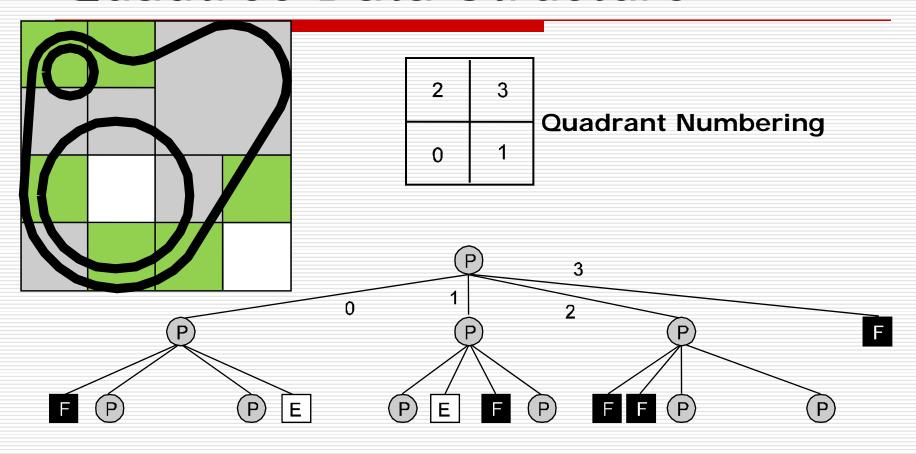


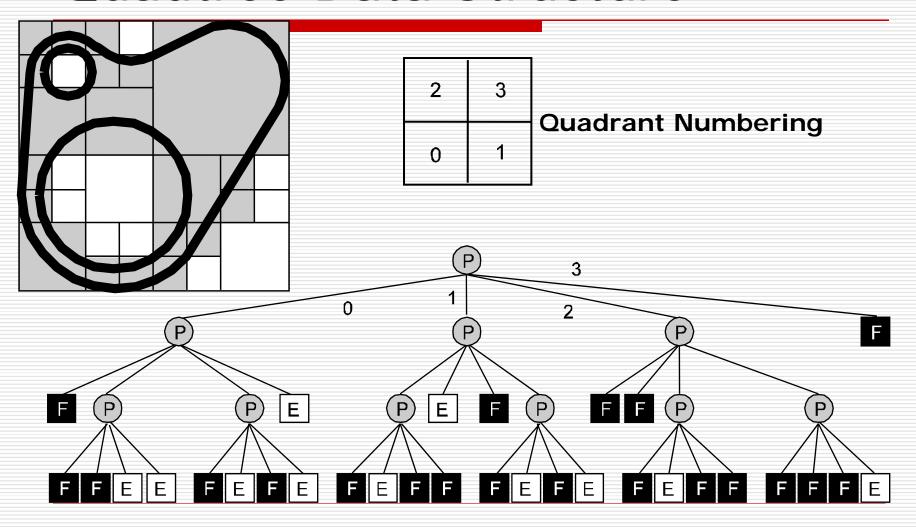
2	3
0	1

Quadrant Numbering

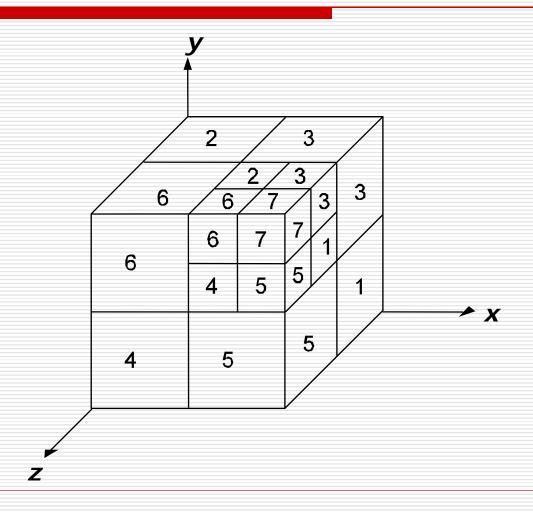


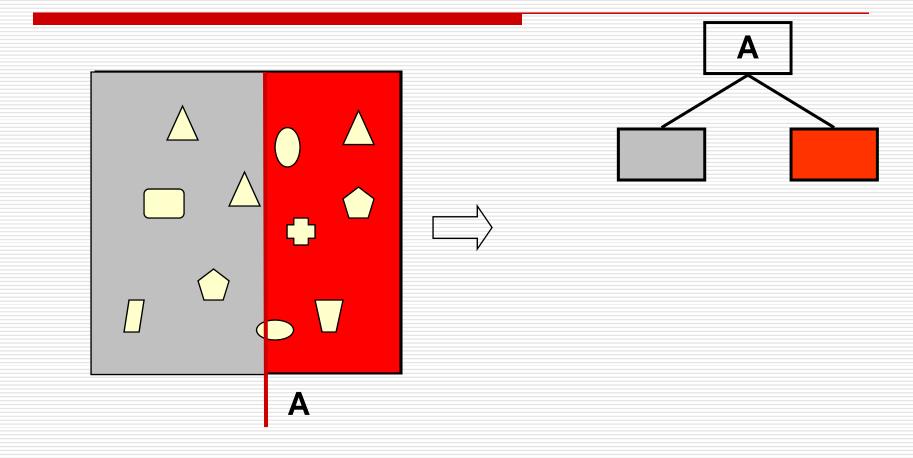




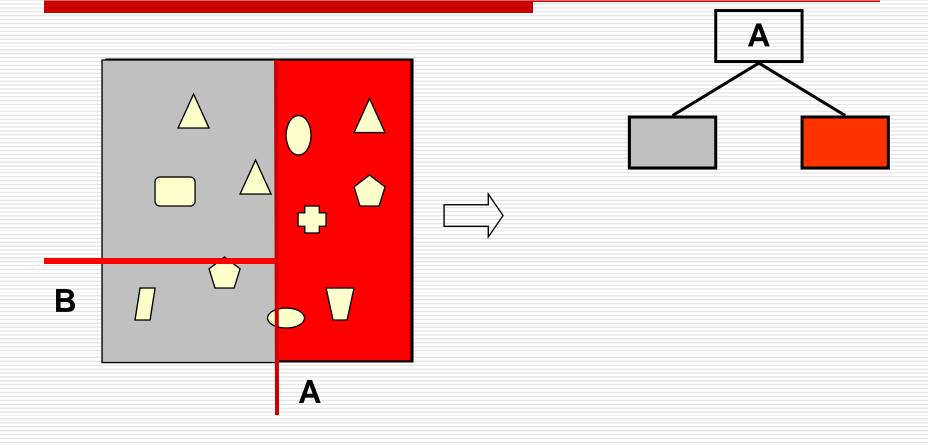


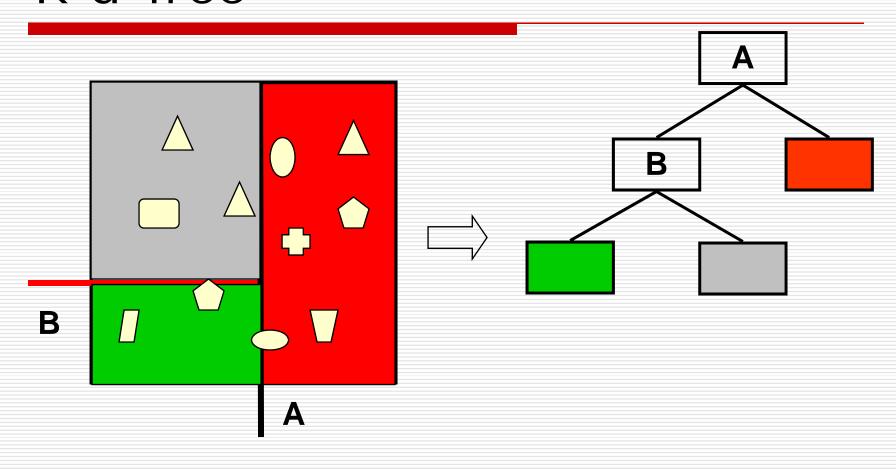
From Quadtree to Octree

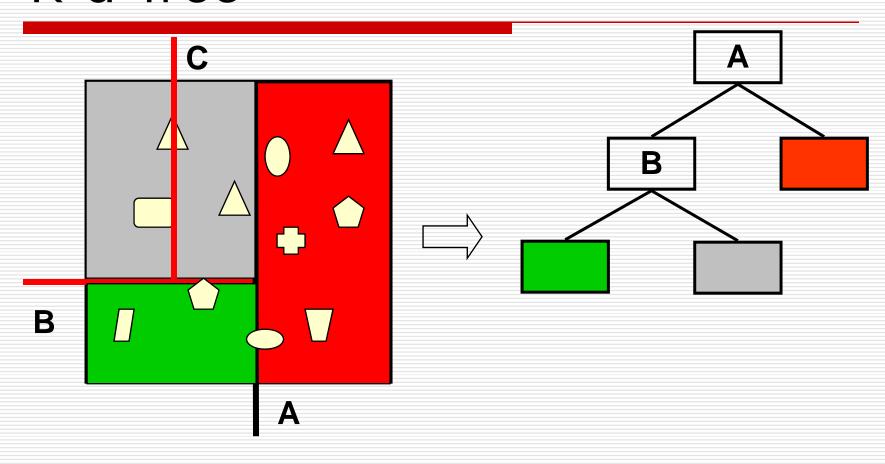


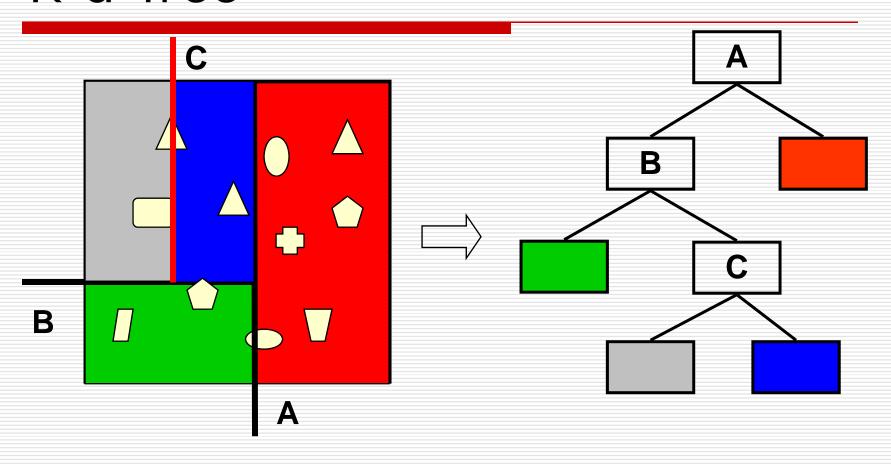


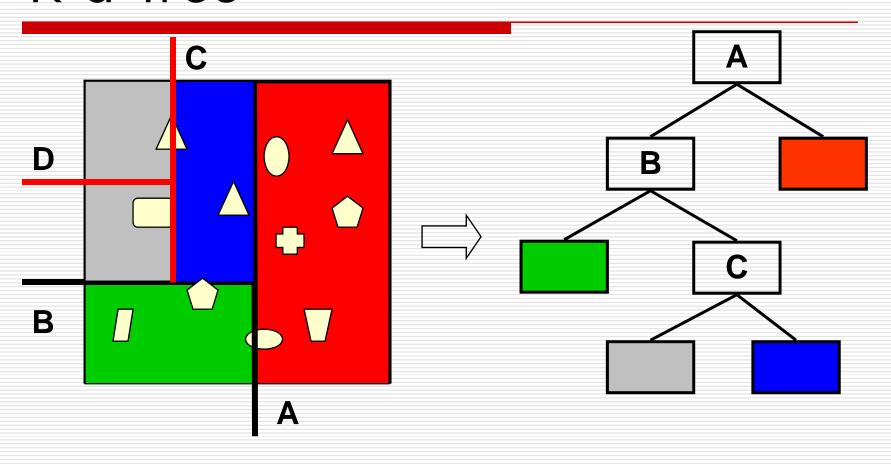
Leaf nodes correspond to unique regions in space

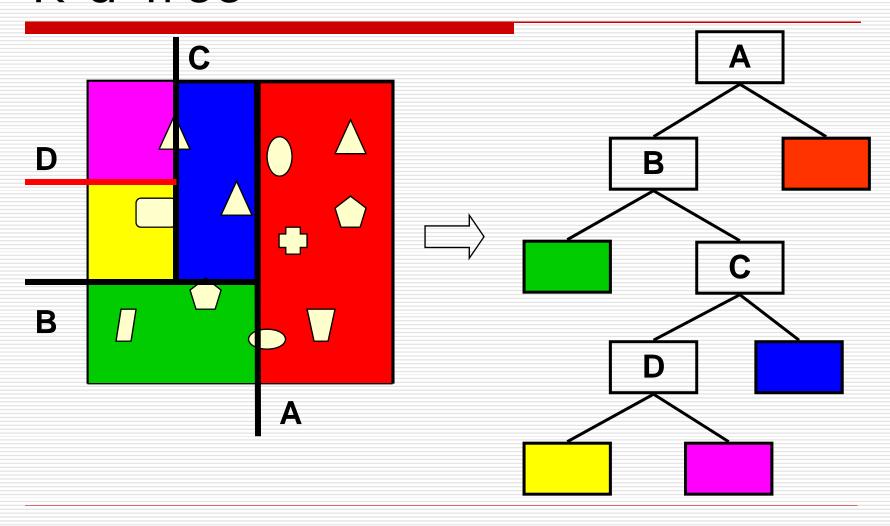


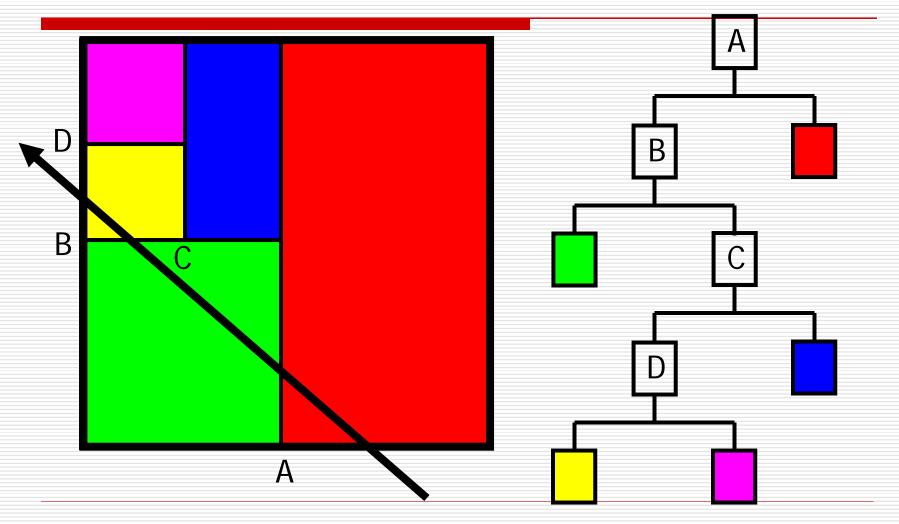






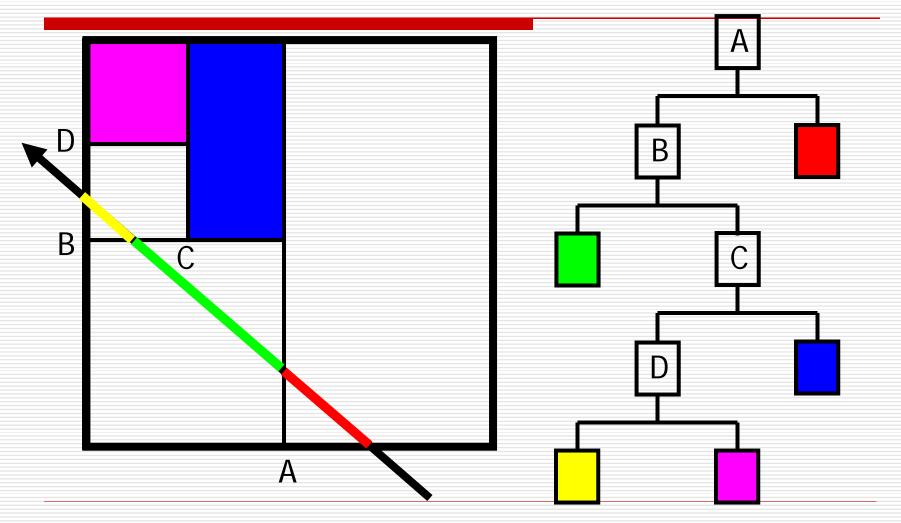






Leaf nodes correspond to unique regions in space

K-d Tree Traversal



Leaf nodes correspond to unique regions in space